

Step 5: Compute strain in compression reinforcement ϵ_{sc} and stress in compression reinforcement σ_{sc}

$$\epsilon_{sc} = 0.0035 \left(1 - \frac{d'}{x_m} \right) = 0.0035 \left(1 - \frac{70}{300} \right) = 2.7 \times 10^{-3}$$

From table of stresses σ_{sc} in compression steel

$$\therefore \sigma_{sc} = 353 \text{ N/mm}^2$$

Step 6: Compute area of compression steel

$$A_{sc} = \frac{M - M_{lim}}{\sigma_{sc} (d - d')} = \frac{(576 - 326) \times 10^6 \text{ N-mm}}{353(630 - 70)} = 1265 \text{ mm}^2$$

Step 7: Compute additional area of tension steel

$$A_{t2} = \frac{\sigma_{sc} A_{sc}}{0.87 \sigma_y} = 1237 \text{ mm}^2$$

Step 7: Compute total area of tension steel

$$A_t = A_{t1} + A_{t2} = 1790 + 1237 = 3027 \text{ mm}^2$$

Step 8: Provide reinforcement

Provide 5 - 28 mm bars at bottom ($A_t = 3078 \text{ mm}^2$) and provide 5 - 18 mm bars at top ($A_{sc} = 1272 \text{ mm}^2$).

Step 9: Check for maximum tension steel

$$A_{max} = 0.04bD = 0.04 \times 300 \times 700 = 8400 \text{ mm}^2 > 3078 \text{ mm}^2 \text{ Hence O.K.}$$

Example (SSC, Junior Engineer, 2010, Working stress method)

Determine the maximum superimposed distributed load which the beam section 220 mm x 440 mm (effective cover = 40 mm) reinforced with total area of tension steel 1256.64 mm², can carry, if the effective span is 5 m. Use M20 concrete and Fe 415 steel. Take $m = 13.33$.

Solution

Size of beam = 220 mm x 440 mm

$D = 440 \text{ mm}$ $d = 440 - 40 = 400 \text{ mm}$

$A_{st} = 1256.64 \text{ mm}^2$

Effective depth, $l = 5 \text{ m}$

Design constants

For M20 concrete $\sigma_{cbc} = 7 \text{ N/mm}^2$

For Fe 415 steel, $\sigma_{st} = 230 \text{ N/mm}^2$

$m = 13.33$

Critical depth of neutral axis (x_c)

$$x_c = \frac{m \sigma_{cbc}}{m \sigma_{cbc} + \sigma_{st}} x d = \frac{13.33 \times 7}{13.33 \times 7 + 230} \times 400 = 115.44 \text{ mm}$$